BAYESIAN APPROXIMATION OF RNA FOLDING TIMES

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ABSTRACT

RNA is a dynamic biomolecule with its function largely determined by its folding into complex structures. During the folding process, an RNA traverses through a series of intermediate structural states, with each transition occurring at variable rates that collectively influence the time required to reach the functional form. Understanding these folding kinetics is vital for predicting RNA behavior and optimizing applications in synthetic biology and drug discovery. While in silico kinetic RNA folding simulators are often computationally intensive and time-consuming, accurate approximations of the folding times can already be very informative to assess the efficiency of the folding process. Here, we present KinPFN, a novel approach that leverages prior-data fitted networks to directly model the posterior predictive distribution of RNA folding times. Trained on synthetic data representing arbitrary prior folding times, KinPFN efficiently approximates the cumulative distribution function of RNA folding times in a single forward pass, given only a few initial folding time examples. Our method offers a modular extension to RNA kinetics algorithms, promising significant computational speed-ups orders of magnitude faster, while achieving comparable results.

1 Introduction

Ribonucleic acid (RNA) plays a pivotal role in various biological processes, serving as a crucial intermediary between DNA and proteins while exerting significant regulatory functions through diverse mechanisms (Fu, 2014). Composed of four nucleotides — Adenine (A), Cytosine (C), Guanine (G), and Uracil (U) — the functionality of RNA is closely tied to its structure (Lodish et al., 2005): An RNA molecule adopts one or more native conformations that are essential for its biological activity (Fang et al., 2015). The dynamic process of how RNAs acquire their functional structure is known as the kinetic folding of RNA. During this process, the RNA strand transitions through several intermediate structural states, driven by intra-molecular interactions (Flamm et al., 2000; Yu et al., 2018). Since misfolding can lead to significant dysfunctions (Conlon & Manley, 2017), the study of RNA folding kinetics is highly relevant for biomedical applications.

An important aspect of folding dynamics is the study of the rates and pathways through which RNA molecules achieve their native structures (Chen, 2008). A common measure to quantify these processes are first passage times (FPTs), i.e. the time required to acquire a certain structure for the first time, and their cumulative distribution functions (CDFs) (Flamm et al., 2000; Wolfinger et al., 2004). These functions are derived from extensive simulations, requiring thousands of folding

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iterations to capture the probabilistic behavior of RNA molecules. While essential for understanding RNA dynamics, calculating FPT CDFs is computationally expensive (Wolfinger et al., 2004; Badelt et al., 2023), posing a significant barrier to real-time applications such as kinetic RNA design, which is critical for drug discovery. While deep learning methods could improve the state of the art in RNA folding (Fu et al., 2022; Franke et al., 2024) and RNA design (Runge et al., 2024; Patil et al., 2024), they are not yet used in modeling RNA kinetics.

In this work, we present *KinPFN*, a novel deep learning-based approach that dramatically accelerates the computation of RNA first passage times via in-context learning. *KinPFN* leverages prior-data fitted networks (PFNs) (Müller et al., 2022) trained on synthetic datasets of RNA folding times to predict the entire CDF of folding times from just a few context examples in a single forward pass. By providing fast and accurate distribution approximations, *KinPFN* can be integrated with existing RNA kinetics simulators, offering comparable performance at a fraction of the computational cost.

Our main contributions are summarized as follows:

- We propose a new synthetic prior to sample datasets of RNA folding times. We use this synthetic data to train a prior-data fitted network to learn to predict the distribution of RNA first passage times, conditioned on a small set of context examples (Section 2.1).
- We introduce *KinPFN*, a new deep learning model for RNA kinetics. *KinPFN* provides accurate predictions of RNA first passage time distributions, accelerating kinetic simulations by orders of magnitude (Section 2.2).
- We evaluate *KinPFN*'s performance on synthetic and real-world RNA data, demonstrating its practical utility through two case studies: an analysis of eukaryotic RNAs and a study of RNA folding efficiency (Section 4).

We provide an overview of *KinPFN* in Figure 1. Our source code, data, and trained models are publicly available at https://github.com/automl/KinPFN.

a Training on a Synthetic Prior Synthetic Datasets are Drawn from KinPFN Leverages In-Context Learning KinPFN is Trained on ${\sim}5M$ Multi-Modal Gaussians to Mimic to Approximate a Given Distribution Distributions by Minimizing the RNA Folding Time Distributions from a Few Example "Times" Negative Log-Likelihood Context Riemann Distribution b Application RNA Kinetics Simulators are KinPFN Approximates the KinPFN Achieves Comparable Costly and Scale Exponentially Distribution of Folding Times Using Results While Reducing with the RNA Length Kinetics Simulations data as Context Simulator Costs by $\geq 95\%$ Simulator Data KinPFN Approximation Runtime Folding Time Simulator KinPFN Length

Figure 1: Graphical abstract. **a**: *KinPFN* is trained on synthetic RNA folding time distributions drawn from parameterized multi-modal Gaussians by minimizing the negative log-likelihood (NLL). **b**: *KinPFN* accelerates RNA kinetics simulators by predicting the RNA folding time distribution in a single forward pass, given a few folding times as context.

2 APPROXIMATION OF RNA FOLDING TIME DISTRIBUTIONS

The first passage time t is the time required for the RNA $\phi \in \{A,G,C,U\}^l$ of length l to fold from an initial structure ω_{start} into a stop structure ω_{stop} while transitioning through arbitrary intermediate structural states. Running M folding simulations under the same conditions (for RNA sequence ϕ , ω_{start} , and ω_{stop}) yields distinct first passage times t_1,\ldots,t_M . By aggregating these times, we compute the fraction of molecules ϕ folded by time T, denoted $F^{\phi}(T)$, where $F_t^{\phi}(T) = P(t \leq T)$ represents the CDF of the stochastic variable t.

We then consider the problem of learning the posterior predictive distribution (PPD) of first passage times for an RNA molecule ϕ , conditioned on a small set of initial examples, to approximate the cumulative distribution function (CDF): Given $N \ll M$ observed first passage times t_1, \ldots, t_N and a prior distribution over first passage times from which we can generate samples, we aim to approximate the PPD $q(t \mid t_1, \ldots, t_N)$. With an approximated PPD, we can compute the predicted CDF $\hat{F}^{\phi}(T)$, which approximates the true CDF $F^{\phi}(T)$; the fraction of molecules folded by time T.

However, obtaining large amounts of prior RNA kinetics data to train a deep learning model, particularly for longer RNAs, is currently infeasible due to the exponential runtime of accurate kinetic simulators (see Figure 4 in Appendix B). This hinders us from using traditional Bayesian approaches for the approximation of RNA first passage times, e.g. by training a variational autoencoder (VAE) (Kingma, 2013) or a probabilistic transformer (Franke et al., 2022). Therefore, we take an alternative approach, training a prior-data fitted network (PFN) (Müller et al., 2022) on a synthetic prior of RNA first passage time distributions. PFNs use a transformer-based model to perform approximate Bayesian inference. They are trained to predict an output $y \in \mathbb{R}$, conditioned on an input x and a training set D_{train} of input-output pairs. During training, these samples are drawn from a prior distribution over datasets $p(\mathcal{D})$, optimizing the Cross-Entropy loss for a PFN q_{θ} with parameters θ ,

$$\ell_{\theta} = \mathbb{E}_{(x,y) \cup D_{\text{train}} \sim p(\mathcal{D})} \left[-\log q_{\theta}(y \mid x, D_{\text{train}}) \right], \tag{1}$$

for predicting the label y, given x and D_{train} . As shown by Müller et al. (2022), this approach directly minimizes the Kullback-Leibler (KL) divergence between the prediction of the PFN and the true posterior predictive distribution when training on many samples of the form $(x,y) \cup D_{\text{train}}$. In this work, we adapt this strategy to tackle the prediction of RNA first passage time distributions, accounting for the specific challenges of the probabilistic behavior of RNA molecules that is also reflected in kinetic simulators by renouncing quantile information.

2.1 A SYNTHETIC PRIOR FOR RNA FOLDING TIME DISTRIBUTIONS

Developing a synthetic prior for molecular problems is challenging since it seems impossible to generate meaningful synthetic combinations of molecule features with posterior information from a process depending on these features. We, therefore, develop *KinPFN* independent of molecular features and restrict its input to first passage times only. This offers the advantage that we can apply *KinPFN* to predict first passage time distributions at test time, independent of the underlying data-generating process.

For the development of our synthetic FPT prior, we leverage the observation that RNA first passage time distributions often exhibit CDFs with regions of slower growth interspersed with steeper transitions, leading to distinct plateaus and multiple changes between convex and concave sections representing inefficiencies in the corresponding folding pathway (Flamm et al., 2000; Wolfinger et al., 2004). These patterns make multi-modal distributions a natural choice to model the complexity of such processes synthetically, as they are designed to capture data with multiple local maxima or modes (Hartigan & Hartigan, 1985). For this work, we decide to construct a prior distribution over RNA first passage times as a family of multi-modal Gaussian distributions $\{P_{\psi_k} \mid k \in \{2,3,4,5\}, \psi_k \in \Psi_k\}$. Each multi-modal distribution in this family comprises k Gaussian components, each characterized by its own mean μ_i and standard deviation σ_i , $i=1,\ldots,k$. The parameter space Ψ_k thus defines the family of distributions, with each specific distribution parameterized by a vector $\psi_{\mathbf{k}} = ((\mu_1, \sigma_1), (\mu_2, \sigma_2), \ldots, (\mu_k, \sigma_k))$ within Ψ_k . We illustrate a synthetic bi-modal PDF alongside its corresponding CDF and examples of synthetic first passage time CDFs in Figure 5. However, note that we are not limited to Gaussians in the prior formulation but that any family of (multi-modal) distributions could be used as a prior for KinPFN.

Since we cannot make any further assumptions about the distribution of folding times, especially when generating synthetic data, x and y of a prior distribution $p(\psi_k)$ are considered completely independent. Consequently, we decide to assign a value of zero to all variables x, representing no prior information, while the y variables are ultimately sampled from the aforementioned multimodal distributions. As the targets y represent synthetic first passage times, they will be referred to as t from this point forward. We set the range of possible first passage time values $t \sim p(\psi_k)$ to $[10^{-6}, 10^{15}]$, a range that covers a large fraction of possible folding processes based on observations from preliminary kinetic simulations. To mimic realistic first passage time distributions, we choose bounded uniform base means $\mu_i^{\text{base}} \sim \mathcal{U}(-5, 16)$, and uniformly distributed standard deviations $\sigma_i \sim \mathcal{U}(0.1, 4.2)$ based on preliminary experiments. To increase the variability of the prior, we introduce a uniformly distributed shifting parameter $\delta \sim \mathcal{U}(-6, 15)$, which is sampled only once and fixed for all $i=1,\ldots,k$. The final means μ_i are then given by:

$$\mu_i = \mu_i^{\text{base}} + \delta \qquad , \tag{2}$$

with the probability density function (PDF) of the multi-modal Gaussian distribution parameterized by ψ_k expressed as

$$p(\psi_k, x) = \sum_{i=1}^k \exp\left(-\frac{(\log x - \mu_i)^2}{2\sigma_i^2}\right) \qquad , \tag{3}$$

for a value x.

To sample first passage times (FPTs) from these PDFs, we generate the PDF over a logarithmically spaced range of x-values within the provided FPT bounds and employ the inverse transformation method, known as the Smirnov transformation. The required series of calculations to derive the CDF, its quantile function CDF⁻¹, different normalizations to properly scale the functions, and logarithmic transformations are detailed in Appendix C.1. The prior distribution over synthetic RNA first passage times used in this work is then represented by the log-encoded samples from a multi-modal Gaussian distribution $p(\psi_k) \in P_{\psi_k}$:

$$\mathbf{Y} = \log_{10} \left(\left\{ CDF^{-1}(\psi_k) \left(\mathcal{U}(0,1) \right) \mid p(\psi_k) \right\} \right). \tag{4}$$

2.2 PFNs for the Approximation of RNA Folding Time Distributions

We propose to use PFNs (Müller et al., 2022) to accelerate kinetic simulations for RNA first passage time distributions. During training, the PFN q_{θ} with model parameters θ is presented with M synthetic first passage times, $\{(0_i,t_i)\}_{i=1}^M$, sampled from the prior distribution $p(\psi_k)$. To enable the model to generalize across varying amounts of training data instead of a fixed number of context folding times, this example set is split at a random cutoff point $N \sim \mathcal{U}(0, M-1)$, resulting in a training subset $D_{\text{train}} = \{(0_i,t_i)\}_{i=1}^N$, while the remaining first passage times are held out via masking. These held-out times, $t_{\text{test}} = \{t_{N+1}, \ldots, t_M\}$, are then used as targets for prediction by minimizing the prior-data negative log-likelihood (NLL) according to Equation 1:

$$\ell_{\theta} = \mathbb{E}_{(0, t_{\text{test}}) \cup D_{\text{train}} \sim p(\psi_k)} \left[-\log q_{\theta}(t_{\text{test}} | 0_{\text{test}}, D_{\text{train}}) \right]$$
 (5)

Figure 2 schematically illustrates this training process of KinPFN for a single batch of size B, along with its application in approximating the posterior predictive distribution (PPD) of RNA first passage times using N real folding times as context obtained from a kinetic simulator.

KinPFN Architecture and Hyperparameters We adopt the transformer-based (Vaswani et al., 2017) PFN architecture as proposed by Müller et al. (2022) and treat each pair (0,t) as a separate token. To learn the distribution of the targets rather than ordering, we deliberately omit positional encoding to maintain permutation invariance according to Müller et al. (2022). Since the first passage times t have already been log-encoded to the range [-6,15] in the prior distribution $p(\psi_k)$ (see Section 2.1), we encode the input with a linear layer after normalizing the data to zero mean and a standard deviation of one while preserving the distributional properties. Following Müller et al. (2022), we mask the attention matrix such that each position only attends to the training positions. This ensures that only training examples influence the predictions while test samples remain independent. We use the Adam optimizer (Kingma & Ba, 2015) with a cosine decay (Loshchilov & Hutter, 2017) and a linear learning rate warm-up over 25% of the training steps as previously

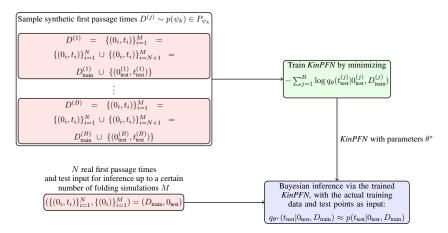


Figure 2: A schematic visualization of KinPFN. Diagram based on Müller et al. (2022).

proposed (Müller et al., 2022; Adriaensen et al., 2023). *KinPFN* outputs a discretized distribution $q_{\theta}(t|0, D_{\text{train}})$ (*Riemann distribution*; see Müller et al. (2022)) using a finite number of buckets with equal likelihood of containing t; a hyperparameter that is included in our hyperparameter optimization (HPO) procedure leading to a final number of 1,000 buckets for *KinPFN*, initialized on a batch of 100,000 prior samples. A visualization of the discretized distribution q_{θ} can be found in Appendix H.4. Further hyperparameters, like the number of layers, the embedding size, or the learning rate are inherited from the Transformer architecture. Given the infinite nature of synthetic training data, we set the dropout rate and the weight decay to zero. We tune hyperparameters in two separate runs using Neural Pipeline search (NePS) (Stoll et al., 2023). More details regarding hyperparameters, hyperparameter optimization, and the final configuration of *KinPFN* can be found in Appendix D. The final model of *KinPFN* was trained for roughly five hours on a single A40 GPU.

3 RELATED WORK

An alternative to *KinPFN* are probabilistic density estimators like kernel density estimation (KDE) (Bishop, 2006), Gaussian Mixture Models (GMM) (Bishop, 2006) or Bayesian Gaussian Mixture Models, also known as Dirichlet Process GMMs (DP-GMM), which utilize a Variational Bayesian estimation of Gaussian mixtures (Blei & Jordan, 2006). From a deep learning perspective, methods based on normalizing flows (Rezende & Mohamed, 2015), variational autoencoders (VAEs) (Kingma, 2013), or a probabilistic transformer as proposed in (Franke et al., 2022), would be well suited for probability density estimation of RNA folding kinetics. However, these methods typically require large amounts of training data which is not available for RNA folding kinetics. Instead, we approach the problem of folding time prediction using a synthetic prior to train a PFN for direct approximation of the CDF of folding time distributions. For more discussions on related work, please see Appendix A.

4 EXPERIMENTS

In this section, we show that KinPFN transfers from synthetic data to data obtained from two different kinetic simulators and demonstrate its practial relevance in a case study on folding efficiency. We report performance in terms of prior-data negative log-likelihood (NLL) between the approximated posterior predictive distribution (PPD) and the true first passage time distribution, mean absolute error (MAE) between the CDF of the approximated PPD $\hat{F}(t)$ and the true target CDF F(t), and Kolmogorov-Smirnov (KS) statistic (see Appendix F). All experiments analyzing runtimes were benchmarked on a single AMD Milan EPYC 7513 CPU with 2,6 GHz. Preliminary evaluations for the predictions on samples from the synthetic prior are shown in Appendix H.1.

KinPFN Transfers to Real-World Scenarios To assess the capabilities of *KinPFN* to transfer from synthetic data to data obtained from kinetic simulators, we create a novel test set of 635 randomly generated RNA sequences with lengths between 15 and 147 nucleotides, run *Kinfold* (Flamm et al.,

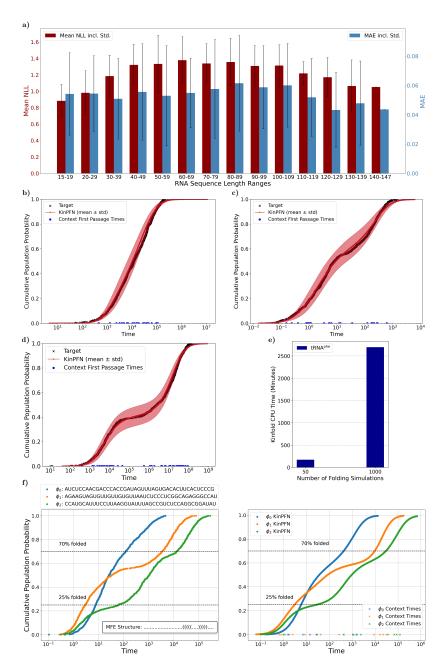


Figure 3: KinPFN approximations of first passage time distributions for simulation data. a) KinPFN testing set PPD mean NLL losses along with the CDF MAEs across RNA sequence length ranges. Error bars show the standard deviation of the losses. b) Example approximation for an alternative folding path of a 75 nucleotide RNA sequence with ground truth data obtained from Kinfold simulations. c) Example approximation for a 56 nucleotide RNA using Kfold simulation data as ground truth. d) KinPFN approximation of the FTP CDF of a $tRNA^{phe}$ using truth = truth

2000) for 1,000 simulations on each of the test samples, and extract first passage times (FPTs) from the simulations. We then analyze the robustness of *KinPFN* to changes in the sequence length of the RNA, the start and stop structure, and a different kinetic simulator, *KFold* (Dykeman, 2015). Additionally, we evaluate *KinPFN* predictions for four types of natural RNAs using *Kinfold* simulations.

Comparisons of *KinPFN* with *GMMs*, *DP-GMMs*, and *KDE* for different context sizes ($N \in \{25, 50, 75, 100, 250, 500, 750, 1000\}$) on our novel testset are shown in Tables 5, 6, 7, 8, 9, and 10 in Appendix H.2. We observe that *KinPFN* outperforms the other approaches across nearly all context first passage times and metrics. Consistent with our expectations, the performance of *KinPFN* constantly improves with more context FPTs. In addition, *KinPFN* seems to generalize across different sequence lengths, start and stop structures, and different simulators as shown in Figure 3a, b, and c. Notably, these approximations with *KinPFN* only require 2,5% of the compute budget of the original simulators to achieve comparable results. However, while we observed robust performance of *KinPFN* for randomly generated RNA sequences, natural RNAs might show different folding behavior compared to random RNA sequences due to million years of evolutionary pressure (Vicens & Kieft, 2022; Herschlag, 1995). As shown in Figure 3d, *KinPFN* is capable of approximating the ground truth data of a tRNA^{phe} nearly perfectly using only 50 context first passage times; a $\sim 20 \times$ speed-up at comparable performance (see Figure 3e). Similar results for further RNA types, are shown in Appendix H.5 and H.6.

Case Study: RNA Folding Efficiency Analysis To demonstrate the utility of KinPFN, we conduct a case study focused on comparing the folding efficiency of three 43 nucleotide long RNA molecules (ϕ_0, ϕ_1, ϕ_2) that are predicted to fold into the same minimum free energy (MFE) structure. Alterations in the RNA sequences, such as mutations or modifications, can have a significant effect on the folding dynamics (Flamm et al., 2000). A comparison of the CDFs of first passage times can distinguish molecules that fold more or less efficiently and provide information about how alternations in the molecules impact the folding behavior, an important aspect for RNA-based therapeutics (Mollica et al., 2022). For our experiment, we simulate 1,000 folding trajectories from the open chain to the MFE structure using Kinfold and calculate the ground truth first passage time CDFs shown in the left plot of Figure 3f for each of the three RNA molecules.

We find that *KinPFN* captures the general folding behavior of the RNAs accurately, as shown in Figure 3f (right). However, while it captures the saddle points of the CDFs of ϕ_1 (orange) and ϕ_2 (green) arguably well, it is slightly less accurate for the most efficiently folding RNA, ϕ_0 (blue). Remarkably, the *KinPFN* approximations were obtained using only ten context times, marking a $100\times$ speed-up compared to each of the three individual simulation trajectories. Results for more approximations using different context lengths are shown in Appendix H.7.

5 CONCLUSION, LIMITATIONS & FUTURE WORK

We present *KinPFN*, the first work that uses prior-data fitted networks for biological data. Trained on a synthetic prior, we show that our novel approach can accurately model RNA folding kinetics while accelerating RNA first passage time analysis by orders of magnitude.

Limitations While showing impressive accuracy, *KinPFN* also has limitations. Generally, it depends on a data-generating approach like kinetic simulators during inference. Consequently, *KinPFN*'s performance is bounded by the accuracy of the simulator. Incorporating other features, like the RNA sequence, structure, or energy information, could mitigate this issue. However, it is an open problem to implement the required information in a synthetic prior without using external data sources. Additionally, larger-scale evaluations, e.g., on longer RNAs, would confirm its independence of RNA features like sequence length. However, obtaining this kind of data is currently infeasible due to the large computing demands of available simulators and the problem's complexity. Finally and similar to GMMs and KDEs, the performance of *KinPFN* strongly depends on the provided context. We tried to compensate for that by showing mean and standard deviation around the mean across 20 context inputs to quantify the variation in *KinPFN* approximations.

Future Work Using synthetic data for biological applications appears very promising. Unlike GMMs or standard KDEs, *KinPFN* is not limited to predefined kernels or Gaussian distributions; we consider the definition of synthetic priors using different distributions as future work.

SOURCE CODE AND REPRODUCIBILITY OF RESULTS

To ensure the reproducibility of our results, we have made our source code, the trained model, and datasets publicly available at https://github.com/automl/KinPFN. The repository contains detailed instructions for setting up the required conda environment and package installs (see README.md). Model checkpoints of *KinPFN* are provided in the models directory. The validation and test sets are stored in the neps_validation_set and kinpfn_testing_set directories, respectively. We provide notebooks (along with the required experiment data) to demonstrate the training and evaluation of *KinPFN* and for reproducing results in the notebooks directory. We recommend using a single GPU with at least 48GB of memory for training *KinPFN*. However, for inference, a single CPU should be sufficient. Following the provided instructions, it should be straightforward to reproduce our environment, train and evaluate *KinPFN*, and replicate our experiments with minimal effort.

AUTHOR CONTRIBUTIONS

F.R. conceptualized the study and developed the methodology. D.S. and F.R. wrote the manuscript, designed figures, and were responsible for data curation. D.S. implemented the model and conducted all experiments. J.F. contributed to the experimental design and baseline selection. M.W. and C.F. provided expertise in RNA kinetics simulations and theory. J.F., M.W., and C.F. assisted with manuscript refinement and figure layout. F.H. provided project supervision and secured funding.

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A FURTHER BACKGROUND & RELATED WORK

In the following, we outline further background information and related work on RNA folding dynamics.

The folding dynamics of RNA can be described as a stochastic process in a state space, comprised of a set of structures or conformations a given RNA sequence may assume, a move set that defines the allowed elementary transitions between conformations in the state space, and transition rates for all allowed transitions. Mathematically, this compiles into a continuous time Markov process governed by the following master equation for the state probabilities $P_x(t)$ of observing state x at time t

$$\frac{dP_x(t)}{dt} = \sum_{y \neq x} [P_y(t)k_{xy} - P_x(t)k_{yx}]$$

where k_{xy} is the transition rate from state y to state x. However, for RNA sequences of moderate length, the master equation becomes too high dimensional to be solved analytically.

Generally, *in silico* analysis of RNA folding kinetics can be divided into nucleotide-resolution and coarse-grained approaches. While the first yields a high level of simulation details, the latter typically allows studying larger systems, i.e. longer RNA chain lengths. The first publicly available tool for computing RNA folding kinetics at nucleotide resolution is *Kinfold* (Flamm et al., 2000), a Markov-chain Monte Carlo (MCMC) method that is still considered one of the most accurate approaches available (Fukunaga & Hamada, 2019). This accuracy, however, comes at the cost of runtime as *Kinfold* MCMC simulations typically require a large number of trajectories to obtain reliable results. While it is possible to simulate the folding kinetics of RNA chains of several hundreds of nucleotides, such calculations require substantial compute (Fukunaga & Hamada, 2019). This limitation inspired accelerating techniques like memoization and parallelization (Aviram et al., 2012), or shortcuts for the energy calculations of RNA secondary structures as implemented in *Kfold* (Dykeman, 2015). In contrast, we develop *KinPFN* as an extension to existing kinetic RNA folding simulators to massively speed up every kinetic simulator that produces first passage times.

A different approach to simulating the dynamics of RNA folding is through analysis of the underlying folding landscape. Such a landscape can be constructed from complete suboptimal folding with *barriers* (Flamm et al., 2002), which provides an exact partitioning of the RNA conformation space into basins of attraction, i.e. local optima of the energy landscape. These macro-states provide a natural coarse-graining of the folding landscape and allow to re-formulate the dynamics on a reduced number of states, resulting in a massive speedup of computation time at comparable levels of detail. This idea is implemented in the tool *treekin*, which models the complete folding dynamics of RNA molecules of length up to approximately 100 nucleotides as a continuous-time Markov process that is solved by numerical integration (Wolfinger et al., 2004).

An Alternative to KinPFN are probabilistic density estimators like kernel density estimation (KDE) (Bishop, 2006), Gaussian Mixture Models (GMM) (Bishop, 2006) or Bayesian Gaussian Mixture Models, also known as Dirichlet Process GMMs (DP-GMM), which utilize a Variational Bayesian estimation of Gaussian mixtures (Blei & Jordan, 2006). Similar to KinPFN, GMM and DP-GMM aim to model the posterior predictive distribution as a multi-modal Gaussian distribution. While GMMs struggle with complex data structures, especially when the number of modes is unknown, Bayesian approaches like DP-GMM can dynamically adjust the number of mixture components (McLachlan et al., 2019; Neal, 2000). Alternatively, kernel density estimation (KDE) offers a non-parametric approach by estimating probability densities through the summation of kernels, like Gaussians, over data points (Bishop, 2006). From a deep learning perspective, methods based on normalizing flows (Rezende & Mohamed, 2015), variational autoencoders (VAEs) (Kingma, 2013), or a probabilistic transformer as proposed in (Franke et al., 2022), would be well suited for probability density estimation of RNA folding kinetics. However, these methods typically require large amounts of training data which is not available for RNA folding kinetics. Instead, we approach the problem of folding time prediction using a synthetic prior to train a PFN for direct approximation of the CDF of folding time distributions.

For molecular dynamics (MD) simulations, AI methods have already been applied in different parts of the MD pipeline. Deep learning methods like graph neural networks (GNNs) (Gilmer et al., 2017) or variational autoencoders (VAEs) (Kingma, 2013), as well as reinforcement learning (RL) (Sutton, 2018) are regularly used in these scenarios to e.g. enhance the sampling techniques during

MD simulations, replace quantum mechanical force field simulations, or analyze the MD trajectories (Prašnikar et al., 2024). However, current approaches mainly focus on small molecule data due to the complexity of MD simulations for larger macromolecules and have the disadvantage that they require large amounts of simulation data for training (Prašnikar et al., 2024). For more information on AI-based methods in the field of MD simulations, we refer the interested reader to a detailed review of the field by Prašnikar et al. (2024).

While, to the best of our knowledge, *KinPFN* is the first deep learning approach for RNA folding kinetics, PFNs were previously applied to multiple problems like few shot image classification (Müller et al., 2022), classification for small tabular datasets (Müller et al., 2022; Hollmann et al., 2023), extrapolation of learning curves (Adriaensen et al., 2023), Bayesian optimization and hyperparameter optimization (Müller et al., 2023; Rakotoarison et al., 2024), and time series forecasting (Dooley et al., 2024).

B EXPONENTIAL Kinfold RUNTIME

Figure 4 shows the mean CPU times (in minutes), along with the upper bound standard deviations, for simulating 10, 25, 50, 75, and 1000 folding processes — transitioning from an open chain to the minimum free energy conformation — with the mean times calculated for different RNA sequence lengths based on 50 distinct artificial RNA molecules per length. Despite the logarithmic scale on the CPU time axis, the mean CPU time still shows a linear increase, highlighting the exponential growth in the computational time required for these simulations. The calculations for Figure 4 were performed on a single core of an AMD Milan EPYC 7513 CPU with 2.6 GHz.

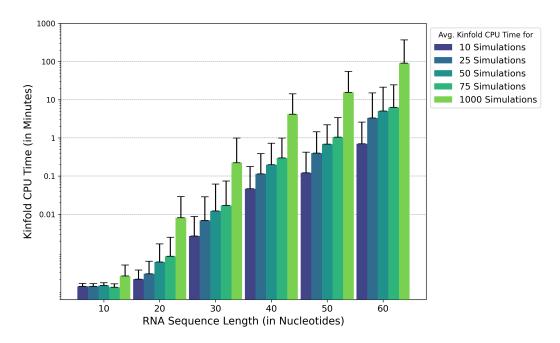


Figure 4: *Kinfold* mean CPU times (in minutes), including the upper bound standard deviations for simulating 10, 25, 50, 75, and 1000 folding processes over different RNA sequence lengths, based on 50 distinct artificial RNA molecules per length.

C SYNTHETIC FOLDING TIME DISTRIBUTION PRIOR DETAILS

In the following, we will describe our proposed synthetic prior and the method for sampling a single batch of synthetic first passage times from it in more detail. The synthetic first passage times t are sampled from a distribution $p(\psi_k)$ generated from a family of multi-modal distributions P_{ψ_k} as introduced in Section 2.1. The possible first passage time values across all $p(\psi_k)$ range from 10^{α} to 10^{β} , with $\alpha=-6$ and $\beta=15$, thereby limiting $T\in [T_{\text{start}},T_{\text{stop}}]$ by $\min(T_{\text{start}})=10^{-6}$ and $\max(T_{\text{stop}})=10^{15}$, as we observed that this time range covers a very high fraction of possible RNA folding processes.

Each distribution $p(\psi_k) \in P_{\psi_k}$ is characterized by k Gaussian components, each with a mean μ_i and a standard deviation σ_i , for $i=1,\ldots,k$. The base means μ_i^{base} are uniformly distributed between $\alpha+1=-5$ and $\beta+1=16$, and the standard deviations σ_i are uniformly distributed between 0.1 and $\frac{\beta-\alpha}{5}=4.2$. Further, we introduce a shifting parameter δ , which is uniformly distributed between α and β , i.e., $\delta \sim \mathcal{U}(-6,15)$ and is fixed for all $i=1,\ldots,k$. The final means μ_i are then given by:

$$\mu_i = \mu_i^{\text{base}} + \delta.$$

Given the parameters ψ_k and a value x, the probability density function (PDF) of the multi-modal Gaussian distribution is expressed as:

$$p(\psi_k, x) = \sum_{i=1}^k \exp\left(-\frac{(\log x - \mu_i)^2}{2\sigma_i^2}\right).$$

C.1 SAMPLING FROM THE SYNTHETIC PRIOR OF RNA FIRST PASSAGE TIMES

To sample a batch of synthetic first passage times of size B with a fixed number of times, i.e., number of simulations per training example of M from a multi-modal distribution $p(\psi_k)$, we employ the inverse transformation method also known as the Smirnov transformation. To do so we generate the PDF $p(\psi_k, x)$ over a logarithmically spaced sequence x of length M from 10^{α} to 10^{β} . Then, to normalize this PDF and therefore ensure a valid probability distribution, we calculate:

$$\hat{p}(\psi_k, x) = \frac{p(\psi_k, x)}{\int_{10^{\alpha}}^{10^{\beta}} p'(\psi_k, \tau) d\tau}.$$
(6)

Next, we compute the cumulative distribution function (CDF)

$$CDF(\psi_k, x) = \int_{10^{\alpha}}^{x} \hat{p}(\psi_k, \tau) d\tau.$$
 (7)

To ensure the CDF ranges from 0 to 1, we normalize it by dividing by the integral over the entire range from 10^{α} to 10^{β} :

$$CDF(\psi_k, x) = \frac{\int_{10^{\alpha}}^{x} \hat{p}(\psi_k, \tau) d\tau}{\int_{10^{\alpha}}^{10^{\beta}} \hat{p}(\psi_k, \tau) d\tau}.$$
 (8)

This normalization ensures that the CDF is properly scaled, with $CDF(\psi_k, 10^{\beta}) = 1$.

By inverting the CDF, we obtain the quantile function $CDF^{-1}(\psi_k)$. To generate samples, we draw uniform samples u_i from a uniform distribution $\mathcal{U}(0,1)$ for $i=1,\ldots,M$ and transform these samples using the inverse CDF:

$$t_i = CDF^{-1}(\psi_k, u_i),$$

where t_i are the sampled values from the distribution. We then encode these samples by applying a logarithmic transformation:

$$\hat{t}_i = \log_{10}(t_i).$$

Finally, constructing the prior output, for a batch of size B and a fixed number of first passage times per example M, we generate the independent variables X and Y as follows:

$$\mathbf{X} = \mathbf{0}_{B imes M imes 1},$$
 $\mathbf{Y}_{i.:} = [\hat{t}_1, \hat{t}_2, \dots, \hat{t}_M] \quad ext{for } i = 1, \dots, B.$

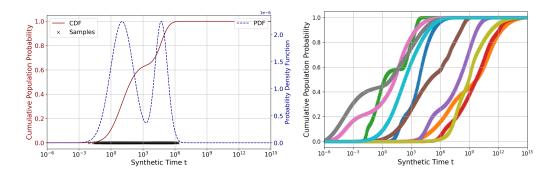


Figure 5: Examples of the synthetic prior of RNA first passage times. We show an example of a single CDF (red) and the corresponding multi-modal probability density function (PDF) (blue; dotted line) generated from the synthetic prior (left). The distribution is bi-modal (k=2) with the parameters $\psi_k=((10.86,1.36),(2.38,2.48))$. The right plot visualizes ten example CDFs generated from the synthetic prior.

D KinPFN DETAILS

D.1 KinPFN HYPERPARAMETER

All hyperparameters in the *KinPFN* model are inherited from the transformer-based architecture (Vaswani et al., 2017) of prior-data fitted networks (PFNs) as proposed by Müller et al. (2022). These include the number of layers (*nlayers*), attention heads (*nheads*), embedding size (*emsize*), the number of neurons in each hidden layer (*nhidden*), the learning rate for the Adam optimizer (Kingma & Ba, 2015) (*learning_rate*), the number of steps per epoch (*steps*), and the total number of epochs (*epochs*). However, it is not entirely accurate to refer to "epochs" in this context, as we are training on synthetic data sampled from a prior, resulting in a single, infinite epoch. In the context of PFNs, the loss is updated after each step, which is why we describe these steps as hyperparameterized steps per epoch. The term "epochs" is used here primarily because it serves as a hyperparameter within the code, providing a mechanism to control the training process. Another crucial parameter is the sequence length (*seq_len*) of the input, representing the number of folding simulations (i.e., first passage times M) fed into the Transformer. This sequence length indicates the number of samples drawn from a prior distribution $p(\psi_k) \in P_{\psi_k}$, as defined in Section 2.1. Additionally, given the infinite nature of synthetic training data and the singular epoch, we set the dropout rate and the weight decay to zero.

D.2 HYPERPARAMETER OPTIMIZATION

Given the uncertainty about the significance of each parameter in the final model's performance, we decided to utilize Neural Pipeline Search (NePS) (Stoll et al., 2023) for the hyperparameter optimization (HPO) of the *KinPFN* architecture. NePS is an open-source Python library that offers state-of-the-art HPO methods, including Bayesian Optimization and multi-fidelity methods like Hyperband (Li et al., 2017). In our setup, we chose Hyperband as our HPO technique. Hyperband optimizes the search process by dynamically allocating resources, enabling faster identification of the best configurations. It strikes an effective balance between exploration and exploitation. Initially, it explores a wide range of configurations with minimal resources, then progressively concentrates resources on the most promising candidates while discarding poor-performing ones early through a process of successive halving (Li et al., 2017).

As a performance metric for Hyperband to assess the quality of hyperparameter configurations, we utilize the prior-data negative log-likelihood (NLL). This approach is equivalent to calculating the Kullback-Leibler divergence between the approximated posterior predictive distribution (PPD) and the true target PPD (Müller et al., 2022). Each configuration trained by Hyperband is evaluated on a newly introduced validation set, discribed in Section G.

We conducted two final iterations of the NePS Hyperband process, evaluating a total of 261 configurations. After completing the first iteration, we made slight adjustments to the search space. Additionally, we set N=25 for the validation pipeline in the first iteration and N=10 for the second iteration, representing the number of context first passage times for each approximation. To ensure comparability across the validation of different hyperparameter configurations, we fixed the indices of these N context first passage times within the available time points, which, in a real-world scenario, would typically be randomized since first passage times are usually obtained without any order when running kinetic folding algorithms like Kinfold (Flamm et al., 2000).

Table 1 and 2 outline the hyperparameter search space used for our optimization process in iteration one and two, respectively (differences are highlighted in blue). In the first iteration, we used a fixed batch size of 50. However, in the second iteration, we reduced the batch size to 40 to accommodate the adjusted search space, which brought us to our GPU memory limit. Since Hyperband requires a fidelity parameter to represent resource usage — in this case, computing time — we designate the *epochs* hyperparameter as the fidelity parameter, defining its range between 250 and 3000. This is directly related to the *steps* per epoch, as the model runs a specified number of steps during each epoch, with each step involving training on a single batch. By tuning both the number of epochs and steps per epoch, we control the amount of synthetic data sampled from the prior that our model sees during training. Additionally, we adjust the learning rate for the Adam optimizer (Kingma & Ba, 2015), setting a range between 10^{-5} and 10^{-3} . This range is informed by preliminary training sessions, where we observed that higher learning rates resulted in highly irregular learning curves

Table 1: Hyperparameter search space for NePS Hyperband iteration 1. Differences to iteration 2 are highlighted in blue

Hyperparameter	Type	Values/Range
epochs	Integer	[250, 3000] (hyperband fidelity)
steps	Integer	[50, 100]
learning_rate	Float	$[10^{-5}, 10^{-3}]$ (log scale)
seq_len	Categorical	{200, 300, 500, 700}
buckets	Categorical	{100, 1000, 10000}
emsize	Categorical	{256, 512}
nheads	Categorical	$\{4, 8\}$
nhidden	Categorical	{512, 1024}
nlayers	Categorical	$\{2, 3, 4, 6, 8, 12\}$

Table 2: Hyperparameter search space for NePS Hyperband iteration 2. Differences to iteration 1 are highlighted in blue

Hyperparameter	Type	Values/Range
epochs	Integer	[250, 3000] (hyperband fidelity)
steps	Integer	[50, 100]
learning_rate	Float	$[10^{-5}, 10^{-3}]$ (log scale)
seq_len	Categorical	{200, 300, 500, 700, 1000, 1400}
buckets	Categorical	{100, 1000, 5000, 10000}
emsize	Categorical	{256, 512}
nheads	Categorical	$\{4, 8\}$
nhidden	Categorical	{512, 1024}
nlayers	Categorical	$\{2, 3, 4, 6, 8\}$

and, consequently, poor performance. We also evaluate models using different Transformer input sequence lengths — specifically 200, 300, 500, 700, 1000, and 1400 — as this parameter represents the number of first passage time samples M drawn from each prior distribution $p(\psi_k)$. Furthermore, we assess the models with 100, 1000, 5000, and 10000 buckets over which we discretize the learned posterior predictive distribution. For the embedding size, we evaluate options of 256 and 512, and we asses 4 and 8 Transformer attention heads, which split the embedded input into smaller segments for focused attention. We also explore various model complexities by varying the number of neurons per hidden layer (512 and 1024) and the total number of layers, considering a broad range from 2 to 12 layers.

After both Hyperband iterations we identified four highly promising KinPFN architectures $\{KinPFN_1, \dots KinPFN_4\}$. Among these, $KinPFN_1$ and $KinPFN_3$ demonstrated the minimal NLL in the first and second NePS Hyperband iteration with 1.1761 (N=25) and 1.2101 (N=10), respectively. Table 3 shows the NLL performance metrics of the found configurations across various cutoffs $N \in \{10, 25, 50, 75, 100\}$. For each distribution example in the proposed validation set, we randomly selected the N context times from the pool of M=1000 available times, ensuring a broader and more generalizable evaluation, as the Hyperband validation pipeline was only based on fixed N first passage times with fixed indices within M.

While $KinPFN_4$ was the configuration with the second-best mean NLL loss with 1.2102 (N=10) after $KinPFN_3$ in the second NePS iteration, $KinPFN_2$ adopted the configuration of $KinPFN_1$ but trained on a larger Transformer input sequence length of 1400.

In the model analysis, KinPFN_1 shows the best performance with N=10 context first passage times. However, for all other values of N ($N \in \{25, 50, 75, 100\}$), KinPFN_2 surpasses it. Additionally, KinPFN_2 outperforms both models from the second NePS iteration, KinPFN_3 and KinPFN_4 , based on the NLL losses, as demonstrated in Table 3. Based on these results, we selected KinPFN_2 as our final KinPFN model that was utilized in all experiments, as it shows the best overall performance.

Table 3: Comparison of four promising KinPFN hyperparameter configurations identified in two NePS (Stoll et al., 2023), i.e., Hyperband (Li et al., 2017) iterations in terms of prior-data negative log-likelihood loss (lower is better) with context first passage time cutoffs $N \in \{10, 25, 50, 75, 100\}$.

Configuration	Parameters	First Passage Times ${\cal N}$				
		10	25	50	75	100
KinPFN ₁	$\begin{array}{llllllllllllllllllllllllllllllllllll$	1.348	1.254	1.225	1.216	1.210
$KinPFN_2$	$\begin{array}{llllllllllllllllllllllllllllllllllll$	1.378	1.246	1.207	1.195	1.189
KinPFN ₃	$\begin{array}{llllllllllllllllllllllllllllllllllll$	1.384	1.255	1.219	1.208	1.202
KinPFN ₄	$\begin{array}{llllllllllllllllllllllllllllllllllll$	1.418	1.259	1.215	1.202	1.194

Final KinPFN Configuration The final KinPFN model consists of 4.86 million parameters, featuring a total of 8 layers, each with a hidden size of 512, 4 attention heads, an embedding size of 256, a learning rate of $2.5588748050825984 \times 10^{-5}$, and 1000 buckets. The model was trained for 1000 epochs, each consisting of 86 steps (with a batch size of 50), resulting in a total of 4,300,000 seen examples (calculated as 1000 x 86 x 50). Each example comprised M=1400 (synthetic) first passage times from (theoretical) folding simulations, which represent the Transformer input sequence length.

E KDE AND DP-GMM DETAILS

To ensure an optimal comparison of KinPFN with Kernel Density Estimation (KDE) and the Dirichlet Process Gaussian Mixture Model (DP-GMM), we performed a random search hyperparameter optimization (HPO). For KDE, we tuned the bandwidth hyperparameter over a logarithmic search space ranging from 10^{-3} to 10^{1} , while for DP-GMM, we optimized the weight concentration prior within a logarithmic range of 10^{-4} to 10^{2} . Both methods were evaluated using 1,000 configurations, selecting the one with the lowest mean negative log-likelihood on our validation set, consisting of 2,019 real RNA first passage time distributions (Appendix G) using 25 context times for each example. Figure 6 illustrates the HPO results for KDE (left) and DP-GMM (right). As a result of the HPO, we selected a bandwidth of 0.352 with a Gaussian kernel for KDE and a weight concentration prior of 9.79e-4 for DP-GMM and allowed a maximum of 100,000 iterations of Expectation-Maximization (EM).

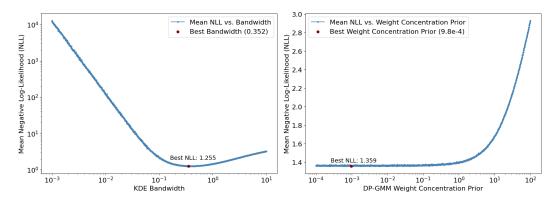


Figure 6: Hyperparameter optimization for Kernel Density Estimation (KDE) on the *bandwidth* parameter (left) and for Dirichlet Process Gaussian Mixture Models (DP-GMM) on the *weight concentration prior* parameter (right).

F METRICS

In our experiments and evaluations, we rely on the prior-data negative log-likelihood (NLL) between the approximated posterior predictive distribution (PPD) and the true first passage time distribution as a primary performance metric, consistent with its use during training and hyperparameter optimization (HPO) (Section 2.2):

$$\ell_{\theta} = \mathbb{E}_{(0, t_{\text{test}}) \cup D_{\text{train}} \sim p(\psi_k)} \left[-\log q_{\theta}(t_{\text{test}} | 0_{\text{test}}, D_{\text{train}}) \right]$$
 (9)

When comparing *KinPFN* to other methods, such as Gaussian Mixture Models (GMM), Dirichlet Process Gaussian Mixture Models (DP-GMM), and Kernel Density Estimation (KDE), we consistently use the mean negative log-likelihood (NLL) as the evaluation metric. This choice is motivated by the fact that the mean NLL reflects how effectively each method has learned the underlying posterior predictive distributions (PPDs) of the first passage times. Minimizing the NLL aligns with minimizing the Kullback-Leibler (KL) divergence between the estimated PPD and the ground truth PPD (Müller et al., 2022), making it a robust measure of model performance.

As our main objective is approximating the CDFs of the first passage times, we additionally evaluate the performance by measuring the mean absolute error (MAE) and Kolmogorov-Smirnov (KS) statistic between the CDF of the approximated PPD $\hat{F}(t)$ and the true target CDF F(t). For a single CDF approximation of KinPFN, the mean absolute error (MAE) is defined as the average of the absolute differences between the predicted CDF values and the ground truth CDF values for a specific sequence of folding times. Mathematically, it can be expressed as:

$$MAE = \frac{1}{M} \sum_{i=1}^{M} |\hat{F}(t_i) - F(t_i)| , \qquad (10)$$

where M is the number of available ground truth first passage time points for the particular example RNA sequence, $\hat{F}(t_i)$ is the predicted CDF value at the i-th first passage time t_i , computed by KinPFN, $F(t_i)$ is the ground truth CDF value at the i-th first passage time t_i .

Similarly, the KS statistic is calculated as the maximum absolute difference between the predicted and true CDFs:

KS Statistic =
$$\max_{y} \left| \hat{F}(t_i) - F(t_i) \right|$$
 ,

where lower values indicate a better fit of the model to the true distribution.

G VALIDATION AND TEST DATA

We introduce two new datasets: a validation set and a test set, both consisting of real RNA first passage times. The validation set contains 2,016 randomly generated RNA sequences, while the test set includes 635 sequences. The times were acquired by simulating the folding process of the RNAs, starting from an open-chain conformation and progressing to the molecule's minimum free energy conformation with the kinetic folding simulator *Kinfold* (Flamm et al., 2000). Figure 7 illustrates the distribution of RNA sequence lengths across both datasets. The validation set, used throughout all NePS (Stoll et al., 2023) iterations (i.e., Hyperband (Li et al., 2017)), is shown in dark blue, while the test set, shown in dark red, is reserved for final *KinPFN* model evaluations (see Section 4). Importantly, these two datasets are mutually independent in terms of RNA primary sequences and secondary structures.

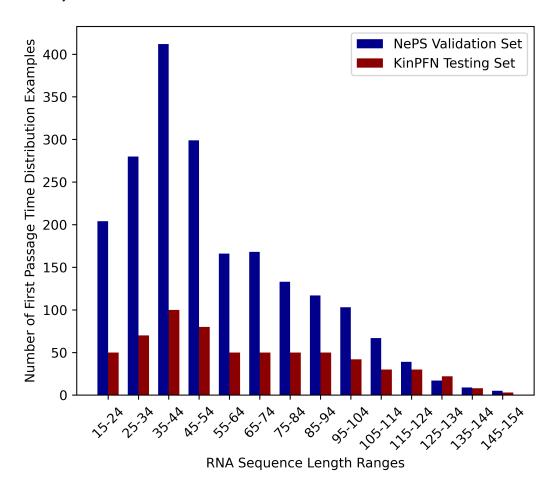


Figure 7: Number of examples by RNA sequence length ranges for the custom validation set used in all NePS (Stoll et al., 2023) i.e., Hyperband (Li et al., 2017) iterations and the custom testing set used for final *KinPFN* model evaluations (Section 4). Both sets are independent of each other with respect to RNA primary sequence and secondary structures.

H ADDITIONAL EVALUATIONS

H.1 SYNTHETIC PRIOR APPROXIMATIONS

We evaluate our proposed model using synthetic data generated from the same prior distribution employed during training (see Section 2.1). We approximate 10,000 synthetic first passage time distributions, varying the cutoff points for the number of context first passage times $N \in \{10, 25, 50, 75, 100\}$. This allows us to evaluate the model's performance as the number of context points provided to KinPFN increases. For each case, we sample M=1000 first passage times from the prior distribution. The performance is measured in terms of the posterior predictive distribution (PPD) mean negative log-likelihood (NLL) and the cumulative distribution function (CDF) mean absolute error (MAE), computed over all 10,000 examples at each cutoff N. Table 4 presents the results of this evaluation. We observe significant improvements in both the NLL and MAE when increasing the number of context points from N=10 to N=25 and from N=25 to N=50. Beyond N=50, while the loss continues to decrease, the rate of improvement slows down as the context size grows from N=75 to N=100.

Table 4: Performance evaluation of $\it KinPFN$ on 10,000 synthetic first passage time distributions. Metrics are shown for different context first passage time cutoffs $N \in \{10, 25, 50, 75, 100\}$, measured in terms of negative log-likelihood (NLL) and mean absolute error (MAE). Lower values indicate better performance.

Performance Metric	First Passage Times N					
	10	25	50	75	100	
Mean Prior-Data NLL Mean Absolute Error	2.4265 0.0878		2.0596 0.0388	2.0388 0.0321	2.0281 0.0275	

H.2 COMPARISON KinPFN, GMM, DP-GMM AND KDE

To further evaluate our model, we compare KinPFN against multiple Gaussian Mixture Models (GMMs) and Dirichlet Process Gaussian Mixture Models (DP-GMMs) using various initial modality assumptions. Specifically, we consider mixture models with modalities $k \in \{2, 3, 4, 5\}$, aligning with the assumptions outlined in our synthetic prior (Section 2.1), denoted as GMM_k and DP- GMM_k . For all evaluations, the models were provided identical context first passage times. Both GMM and DP-GMM models were allowed a maximum of 100,000 iterations of Expectation-Maximization (EM). Additionally, we compare KinPFN to a Kernel Density Estimator (KDE) that we optimized for its bandwidth hyperparameter (Appendix E), as discussed in Section 4. The results for MAE and KS are shown in Table 6 and 7, respectively. We observe that KinPFN outperforms all other methods from context size of 25 FPTs onwards. Results on larger context sizes are shown in Table 8, 9 and 10 demonstrating a constant improvement of the predictions with growing context sizes.

Table 5: Evaluation of *KinPFN*, *KDE*, and multiple GMM_k and DP- GMM_k models with different initial modality assumptions $k \in \{2, 3, 4, 5\}$ on a newly introduced testing set comprising 635 real-world first passage time distributions in terms of prior-data negative log-likelihood loss (lower is better) with context first passage time cutoffs $N \in \{10, 25, 50, 75, 100\}$.

Method	First Passage Times N				
	10	25	50	75	100
KinPFN	1.3739	1.2435	1.2047	1.1916	1.1858
GMM_2	2.3122	1.3612	1.2355	1.2036	1.1933
GMM_3	5.2469	1.5830	1.2838	1.2132	1.1910
GMM_4	13.1325	1.9922	1.3676	1.2480	1.2119
GMM_5	37.5845	2.7708	1.4957	1.2953	1.2374
DP - GMM_2	1.6285	1.3529	1.2618	1.2305	1.2150
DP - GMM_3	1.6268	1.3549	1.2653	1.2323	1.2155
DP - GMM_4	1.6294	1.3558	1.2663	1.2337	1.2169
DP - GMM_5	1.6256	1.3572	1.2675	1.2337	1.2175
KDE	1.4370	1.2559	1.2133	1.2003	1.1957

Table 6: Evaluation of *KinPFN*, *KDE*, and multiple GMM_k and DP- GMM_k models with different initial modality assumptions $k \in \{2, 3, 4, 5\}$ on a newly introduced testing set comprising 635 real-world first passage time distributions in terms of mean absolute error (lower is better) with context first passage time cutoffs $N \in \{10, 25, 50, 75, 100\}$.

Method	First Passage Times N					
	10	25	50	75	100	
KinPFN	0.0843	0.0561	0.0393	0.0333	0.0296	
GMM_2	0.1003	0.0848	0.0790	0.0773	0.0756	
GMM_3	0.0988	0.0866	0.0815	0.0801	0.0778	
GMM_4	0.0952	0.0860	0.0816	0.0799	0.0777	
GMM_5	0.0929	0.0842	0.0809	0.0797	0.0778	
DP - GMM_2	0.0866	0.0774	0.0761	0.0756	0.0745	
DP - GMM_3	0.0867	0.0774	0.0763	0.0762	0.0751	
DP - GMM_4	0.0865	0.0770	0.0763	0.0763	0.0751	
DP - GMM_5	0.0860	0.0768	0.0762	0.0760	0.0751	
KDE	0.0813	0.0690	0.0653	0.0644	0.0630	

Table 7: Evaluation of *KinPFN*, *KDE*, and multiple GMM_k and DP- GMM_k models with different initial modality assumptions $k \in \{2, 3, 4, 5\}$ on a newly introduced testing set comprising 635 real-world first passage time distributions in terms of Kolmogorov-Smirnov (KS) statistic (lower is better) with context first passage time cutoffs $N \in \{10, 25, 50, 75, 100\}$.

Method	First Passage Times N				
	10	25	50	75	100
KinPFN	0.1615	0.1098	0.0809	0.0700	0.0632
GMM_2	0.2084	0.1705	0.1586	0.1541	0.1510
GMM_3	0.2210	0.1794	0.1644	0.1586	0.1537
GMM_4	0.2293	0.1829	0.1674	0.1604	0.1547
GMM_5	0.2352	0.1836	0.1695	0.1625	0.1564
DP - GMM_2	0.1695	0.1505	0.1496	0.1488	0.1471
DP - GMM_3	0.1694	0.1506	0.1499	0.1495	0.1475
DP - GMM_4	0.1691	0.1500	0.1500	0.1496	0.1475
DP - GMM_5	0.1682	0.1494	0.1499	0.1491	0.1476
KDE	0.1590	0.1344	0.1278	0.1256	0.1231

Table 8: Evaluation of *KinPFN*, *KDE*, and multiple GMM_k and DP- GMM_k models with different initial modality assumptions $k \in \{2, 3, 4, 5\}$ on a newly introduced testing set comprising 635 real-world first passage time distributions in terms of prior-data negative log-likelihood loss (lower is better) with context first passage time cutoffs $N \in \{250, 500, 750, 1000\}$.

Method	First Passage Times N					
	250	500	750	1000		
KinPFN	1.1756	1.1716	1.1703	1.1697		
GMM_2	1.1764	1.1715	1.1696	1.1690		
GMM_3	1.1621	1.1542	1.1519	1.1508		
GMM_4	1.1612	1.1506	1.1476	1.1458		
GMM_5	1.1642	1.1499	1.1458	1.1438		
DP - GMM_2	1.1853	1.1735	1.1700	1.1683		
DP - GMM_3	1.1793	1.1627	1.1565	1.1533		
DP - GMM_4	1.1802	1.1631	1.1562	1.1526		
DP - GMM_5	1.1809	1.1637	1.1566	1.1529		
KDE	1.1874	1.1841	1.1832	1.1828		

Table 9: Evaluation of *KinPFN*, *KDE*, and multiple GMM_k and DP- GMM_k models with different initial modality assumptions $k \in \{2, 3, 4, 5\}$ on a newly introduced testing set comprising 635 real-world first passage time distributions in terms of mean absolute error (lower is better) with context first passage time cutoffs $N \in \{250, 500, 750, 1000\}$.

Method	First Passage Times N						
	250	500	750	1000			
KinPFN	0.0205	0.0155	0.0137	0.0126			
GMM_2	0.0742	0.0730	0.0730	0.0728			
GMM_3	0.0764	0.0756	0.0756	0.0754			
GMM_4	0.0763	0.0754	0.0753	0.0751			
GMM_5	0.0762	0.0751	0.0751	0.0747			
DP - GMM_2	0.0746	0.0741	0.0739	0.0736			
DP - GMM_3	0.0760	0.0757	0.0759	0.0757			
DP - GMM_4	0.0759	0.0756	0.0758	0.0756			
DP - GMM_5	0.0759	0.0756	0.0758	0.0756			
KDE	0.0624	0.0617	0.0617	0.0615			

Table 10: Evaluation of KinPFN, KDE, and multiple GMM_k and DP- GMM_k models with different initial modality assumptions $k \in \{2, 3, 4, 5\}$ on a newly introduced testing set comprising 635 real-world first passage time distributions in terms of Kolmogorov-Smirnov (KS) statistic (lower is better) with context first passage time cutoffs $N \in \{250, 500, 750, 1000\}$.

Method	First Passage Times N						
	250	500	750	1000			
KinPFN	0.0484	0.0389	0.0359	0.0336			
GMM_2	0.1482	0.1465	0.1463	0.1460			
GMM_3	0.1493	0.1466	0.1467	0.1462			
GMM_4	0.1489	0.1462	0.1461	0.1454			
GMM_5	0.1499	0.1464	0.1462	0.1454			
DP - GMM_2	0.1474	0.1472	0.1469	0.1465			
DP - GMM_3	0.1483	0.1473	0.1469	0.1463			
DP - GMM_4	0.1481	0.1471	0.1466	0.1461			
DP - GMM_5	0.1482	0.1470	0.1465	0.1460			
KDE	0.1217	0.1205	0.1206	0.1204			

H.3 ADDITIONAL KinPFN APPROXIMATION EXAMPLES

In Section 4, we conducted approximations of first passage time distributions using KinPFN on a 75-nucleotide RNA. The folding process for this RNA was simulated with the Kinfold kinetic simulator (Flamm et al., 2000), employing custom start and stop structures. We also approximated the folding time distribution for a 56-nucleotide RNA, for which we obtained ground truth data using the KFold simulator (Dykeman, 2015). In all instances, the approximations were based on just 25 context first passage times. This appendix provides additional approximations for these RNAs, expanding the analysis by varying the number of context first passage times, specifically $N \in \{10, 25, 50, 75\}$. Additionally, we performed approximations for a 93-nucleotide RNA using the same simulation method as for the 75-nucleotide RNA (Figure 8) and extended our analysis of the 56-nucleotide RNA to include results for a 31-nucleotide RNA (Figure 9). Additionally, Figure 10 presents representative approximations for two RNAs from our newly introduced test set: a 97-nucleotide RNA and a 119-nucleotide RNA, each evaluated with four different numbers of context first passage times, $N \in \{10, 25, 50, 75\}$.

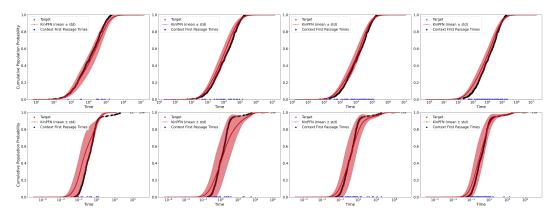


Figure 8: Approximations of the cumulative distribution function (CDF) for the first passage time using KinPFN, with context times $N \in \{10, 25, 50, 75\}$ (left to right), for an RNA sequence of 75 nucleotides (top) and 93 nucleotides (bottom). The folding process was simulated using custom initial and final structures rather than the open chain and minimum free energy conformation.

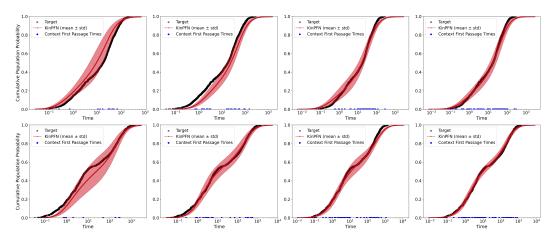


Figure 9: KinPFN first passage time CDF approximations with context times $N \in \{10, 25, 50, 75\}$ (left to right) for a 31 nucleotide long RNA (top) and a 56 nucleotide long RNA (bottom). First passage times were obtained using the kinetic folding algorithm Kfold Dykeman (2015).

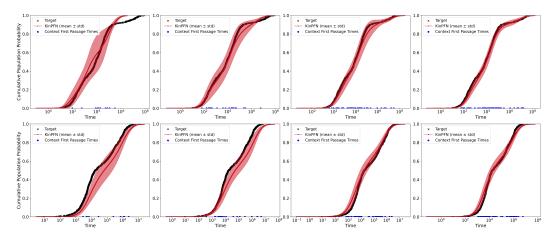


Figure 10: \it{KinPFN} first passage time CDF approximations with context times $N \in \{10, 25, 50, 75\}$ (left to right) for a 97 nucleotide long RNA (top) and a 119 nucleotide long RNA (bottom) that are part of the newly introduced test set.

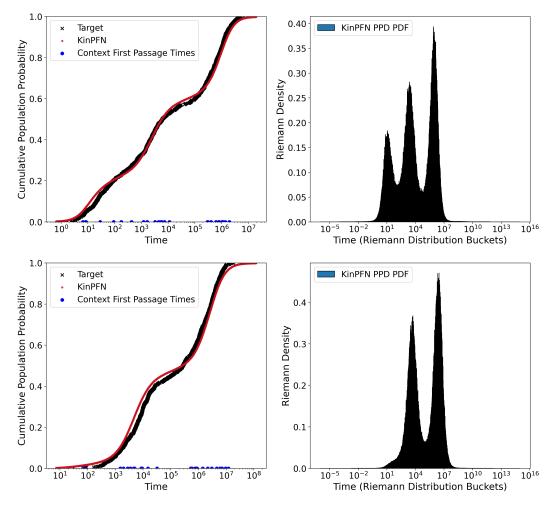


Figure 11: *KinPFN* PPD CDF approximations (left) along with the corresponding multi-modal PPD PDFs (right) for two RNA molecules with lengths of 65 (top) and 86 (bottom) nucleotides.

H.4 KinPFN RIEMANN DISTRIBUTION VISUALIZATION

To provide a more intuitive understanding of the actual KinPFN predictions, Figure 11 illustrates two CDF approximations for different RNA molecules, each with N=25 context first-passage times, compared against the ground truth CDF based on 1,000 Kinfold (Flamm et al., 2000) times (left) alongside the probability density function (PDF) of the corresponding approximated posterior predictive distribution (PPD), also known as the Riemann distribution (right) (Müller et al., 2022). As discussed in Section 2.2, the PFN predicts a continuous distribution, which we discretized into a finite number of buckets, forming the PDF bars. Each bar represents a bucket, and in our final KinPFN model, we used 1,000 buckets, a hyperparameter defined in Section 2.2.

By examining the approximated PPD PDFs, we can observe the multi-modal nature of the learned first-passage time distributions. For instance, the distribution for a 65 nucleotide long RNA in Figure 11 (top) shows bi-modality with two distinct peaks, while another first passage time distribution for a 86 nucleotide long RNA in Figure 11 (bottom) exhibits tri-modality with three peaks. Notably, the calculated CDFs for these multi-modal PPDs align closely with the ground truth CDFs from the 1,000 real first-passage times, demonstrating the effectiveness of our proposed prior, specifically, the family of multi-modal Gaussian distributions introduced in Section 2.1. This prior, from which we sampled synthetic first-passage time distributions to train *KinPFN*, enabled a strong generalization to real-world RNA first-passage time distributions.

H.5 EUKARYOTIC TRANSFER AND RIBOSOMAL RNA

We present additional results for the first passage time distribution approximations using KinPFN for $tRNA^{phe}$ and 5S rRNA from the eukaryote Saccharomyces cerevisiae, also known as brewer's yeast. Figure 13 displays the cumulative distribution function (CDF) approximations of first passage times for $tRNA^{phe}$ (top) and 5S rRNA (bottom), with varying numbers of context first passage times, $N \in \{10, 25, 50, 75\}$, as inputs to KinPFN. Additionally, Figure 12 illustrates the CPU time required (in minutes) to compute 10, 25, 50, 75, and 1,000 first passage times for both $tRNA^{phe}$ (blue) and 5S rRNA (red) using the kinetic simulator Kinfold (Flamm et al., 2000).

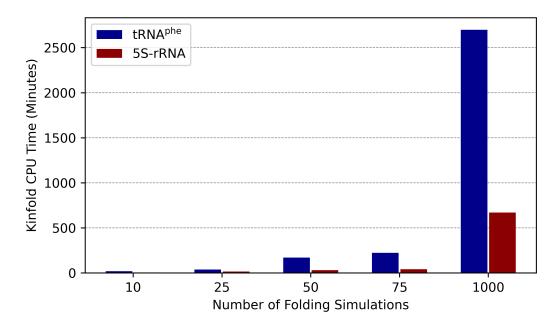


Figure 12: *Kinfold* CPU time (in minutes) vs. number of folding simulations for *Saccharomyces cerevisiae* tRNA^{phe} and 5S rRNA.

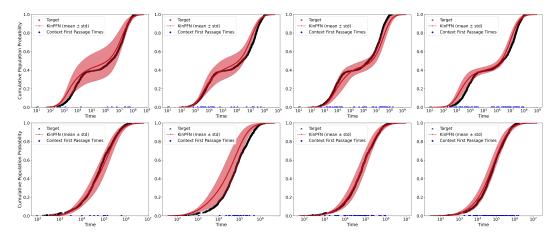


Figure 13: *KinPFN* first passage time CDF approximations with context times $N \in \{10, 25, 50, 75\}$ (left to right) for *Saccharomyces cerevisiae* tRNA^{phe} (top) and 5S rRNA (bottom).

H.6 APPROXIMATIONS FOR ADDITIONAL RNA TYPES

In this section, we show the results of the first passage time distribution approximations using KinPFN on two further RNA types: hsa-miR-7107-3p (RNAcentral-ID: URS0000759FB2_9606) from Homo sapiens (human) and the SAM riboswitch (S box leader) (RNAcentral-ID: URS00002F3927_224308) from Bacillus subtilis subsp. subtilis str. 168. Figure 14 displays the cumulative distribution function (CDF) approximations for the first passage times of these RNAs. The top row shows results for hsa-miR-7107-3p, a 27-nucleotide microRNA, while the bottom row illustrates results for the SAM riboswitch, a 92-nucleotide regulatory RNA. For both RNAs, the approximations are generated using varying numbers of context first passage times as inputs to KinPFN, with $N \in \{10, 25, 50, 75\}$ (from left to right). These results provide additional insights into the robustness and versatility of KinPFN across diverse RNA types.

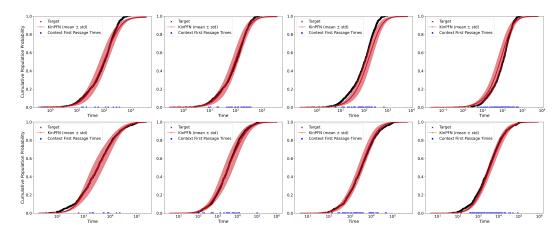


Figure 14: KinPFN first passage time CDF approximations with context times $N \in \{10, 25, 50, 75\}$ (left to right) for a hsa-miR-7107-3p microRNA from $\mathit{Homo \ sapiens}$ (human) (top) and a SAM riboswitch from $\mathit{Bacillus \ subtilis \ subsp. \ subtilis \ str. \ 168}$ (bottom).

H.7 APPLICATION: RNA FOLDING EFFICIENCY ANALYSIS

Here we show KinPFN approximations using additional context first passage times of $N \in \{10, 25, 50\}$ on a case study that focuses on comparing the folding efficiency of three 43-nucleotide RNA molecules (ϕ_0, ϕ_1, ϕ_2) , each predicted to fold into the same minimum free energy (MFE) structure $(\omega_{\text{stop}} = \dots (((((\dots)))))\dots)$. As noted in Section 4, KinPFN accurately cap-

Figure 15: RNA folding efficiency analysis. The first plot from the left shows the ground truth CDFs F(t) for three sequences ϕ_0, ϕ_1 and ϕ_2 , representing the fraction of molecules folded into the MFE conformation over time t. The second, third, and fourth plot displays the KinPFN approximations $\hat{F}(t)$ with ten, 25, and 50 $\mathit{Kinfold}$ times as context.

tures the overall folding behavior of these RNAs using just ten context times. We further observe that increasing the number of context first passage times to 25 and 50 enhances the accuracy of these approximations, as shown in Figure 15.